

# Document made available under the Patent Cooperation Treaty (PCT)

International application number: PCT/CA04/002108

International filing date: 10 December 2004 (10.12.2004)

Document type: Certified copy of priority document

Document details: Country/Office: US

Number: 60/528,775

Filing date: 12 December 2003 (12.12.2003)

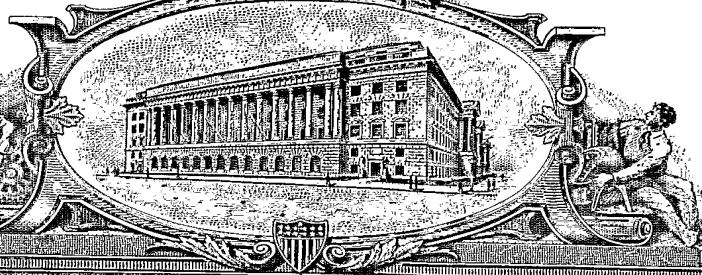
Date of receipt at the International Bureau: 27 April 2005 (27.04.2005)

Remark: Priority document submitted or transmitted to the International Bureau in compliance with Rule 17.1(a) or (b)



World Intellectual Property Organization (WIPO) - Geneva, Switzerland  
Organisation Mondiale de la Propriété Intellectuelle (OMPI) - Genève, Suisse

PA 1163278



# THE UNITED STATES OF AMERICA

TO ALL TO WHOM THESE PRESENTS SHALL COME:

UNITED STATES DEPARTMENT OF COMMERCE

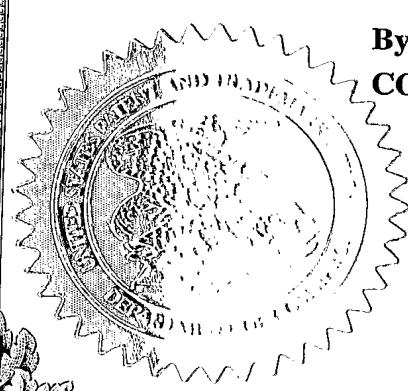
United States Patent and Trademark Office

April 28, 2004

THIS IS TO CERTIFY THAT ANNEXED HERETO IS A TRUE COPY FROM THE RECORDS OF THE UNITED STATES PATENT AND TRADEMARK OFFICE OF THOSE PAPERS OF THE BELOW IDENTIFIED PATENT APPLICATION THAT MET THE REQUIREMENTS TO BE GRANTED A FILING DATE UNDER 35 USC 111.

APPLICATION NUMBER: 60/528,775  
FILING DATE: December 12, 2003

By Authority of the  
COMMISSIONER OF PATENTS AND TRADEMARKS



*P. R. Grant*

P. R. GRANT  
Certifying Officer

PTO/SB/16 (08-03)

Approved for use through 07/31/2008. OMB 0351-0032  
U.S. Patent and Trademark Office: U.S. DEPARTMENT OF COMMERCE**PROVISIONAL APPLICATION FOR PATENT COVER SHEET**

This is a request for filing a PROVISIONAL APPLICATION FOR PATENT under 37 CFR 1.53 (c).

17858 U.S.PTO  
60528775

INVENTOR(S)		
Given Name (first and middle [if any])	Family Name or Surname	Residence (City and either State or Foreign Country)
Samuel Pedro Jerry J.	Goldman Battista	Canada Canada
<input checked="" type="checkbox"/> Additional inventors are being named on the 1 separately numbered sheets attached hereto		
TITLE OF THE INVENTION (600 characters max)		
FAST INVERSE DOSE OPTIMIZATION		
Direct all correspondence to: CORRESPONDENCE ADDRESS		
<input checked="" type="checkbox"/> Customer Number 1059		
OR		
<input type="checkbox"/> Firm or Individual Name		
Address		
Address		
City	State	ZIP
Country	Telephone	Fax
ENCLOSED APPLICATION PARTS (check all that apply)		
<input checked="" type="checkbox"/> Specification Number of Pages 8		
<input type="checkbox"/> Drawing(s) Number of Sheets		
<input checked="" type="checkbox"/> Application Data Sheet. See 37 CFR 1.76		
METHOD OF PAYMENT OF FILING FEES FOR THIS PROVISIONAL APPLICATION FOR PATENT		
<input checked="" type="checkbox"/> Applicant claims small entity status. See 37 CFR 1.27.		
<input type="checkbox"/> A check or money order is enclosed to cover the filing fees		
<input checked="" type="checkbox"/> The Director is hereby authorized to charge filing fees or credit any overpayment to Deposit Account Number: 022095		
<input type="checkbox"/> Payment by credit card. Form PTO-2038 is attached.		
The invention was made by an agency of the United States Government or under a contract with an agency of the United States Government.		
<input checked="" type="checkbox"/> No.		
<input type="checkbox"/> Yes, the name of the U.S. Government agency and the Government contract number are: _____		

Respectfully submitted,  
SIGNATURE 

[Page 1 of 2]

Date

Dec.12/03

TYPED or PRINTED NAME

Timothy J. Simone

REGISTRATION NO.  
(if appropriate)

31,083

TELEPHONE

416-384-7311

Docket Number:

8611-35

**USE ONLY FOR FILING A PROVISIONAL APPLICATION FOR PATENT**  
 This collection of information is required by 37 CFR 1.51. The information is required to obtain or retain a benefit by the public which is to be (and by the USPTO to process) an application. Confidentiality is governed by 35 U.S.C. 122 and 37 CFR 1.16. This collection is estimated to take 8 hours to complete, including gathering, preparing, and filling out and/or maintaining the collection of information. Time will vary depending upon the individual case. Any comments on the amount of time you require to complete this form and/or suggestions for reducing this burden, should be sent to the Chief Information Officer, U.S. Patent and Trademark Office, U.S. Department of Commerce, P.O. Box 1450, Alexandria, VA 22313-1450. DO NOT SEND FEES OR COMPLETED FORMS TO THIS ADDRESS. SEND TO: Mail Stop Provisional Application, Comptroller for Patents, P.O. Box 1409, Alexandria, VA 22313-1450.

If you need assistance in completing the form, call 1-800-PTO-9199 and select option 2.

**PROVISIONAL APPLICATION COVER SHEET**  
*Additional Page*

PTO/SB/16 (08-02)

Approved for use through 07/31/2008, OMB 0651-0032  
Patent and Trademark Office, U.S. DEPARTMENT OF COMMERCE  
Under the Paperwork Reduction Act of 1995, no persons are required to respond to a collection of information unless it displays a valid OMB control number.

Docket Number 9811-35

**INVENTOR(S)/APPLICANT(S)**

Given Name (first and middle [if any])	Family or Surname	Residence (City and either State or Foreign Country)
Jeff Z.	Chen	Canada

[Page 2 of 2]

Number 1 of 1

**WARNING:** Information on this form may become public. Credit card information should not be included on this form. Provide credit card information and authorization on PTO-2038.

16688 U.S. PTO

Under the Paperwork Reduction Act of 1995, no persons are required to respond to a collection of information unless it displays a valid OMB control number.

PTO/SB/17 (10-03)

Approved for use through 07/31/2006, OMB 0651-0032  
U.S. Patent and Trademark Office; U.S. DEPARTMENT OF COMMERCE

# FEE TRANSMITTAL for FY 2004

Effective 10/01/2003. Patent fees are subject to annual revision.

 Applicant claims small entity status. See 37 CFR 1.27

TOTAL AMOUNT OF PAYMENT (\$ 80.00)

## METHOD OF PAYMENT (check all that apply)

 Check  Credit card  Money Order  Other  None
 Deposit Account:

Deposit Account Number 022095  
Deposit Account Name Bereskin & Parr

The Director is authorized to: (check all that apply)  
 Charge fee(s) indicated below  Credit any overpayments  
 Charge any additional fee(s) or any underpayment of fee(s)  
 Charge fee(s) indicated below, except for the filing fee to the above-identified deposit account.

## FEE CALCULATION

## 1. BASIC FILING FEE

Large Entity Fee Code (\$)	Small Entity Fee Code (\$)	Fee (\$)	Fee Description	Fee Paid
1001 770	2001 325	Utility filing fee		
1002 340	2002 170	Design filing fee		
1003 630	2003 265	Plant filing fee		
1004 770	2004 385	Reissue filing fee		
1005 180	2005 80	Provisional filing fee	80.00	
<b>SUBTOTAL (1)</b>		<b>(\$ 80.00)</b>		

## 2. EXTRA CLAIM FEES FOR UTILITY AND REISSUE

Large Entity Fee Code (\$)	Small Entity Fee Code (\$)	Extra Claims	Fee from Examiner	Fee Paid
Total Claims		> 20 * =		0.00
Independent Claims		- 3 * =		0.00
Multiple Dependent				

Large Entity Fee Code (\$)	Small Entity Fee Code (\$)	Fee Description	Fee Paid
1202 18	2202 9	Claims in excess of 20	
1201 66	2201 43	Independent claims in excess of 3	
1203 290	2203 145	Multiple dependent claim, if not paid	
1204 66	2204 43	** Reissue independent claims over original patent	
1205 18	2205 9	** Reissue claims in excess of 20 and over original patent	
<b>SUBTOTAL (2)</b>		<b>(\$ 0.00)</b>	

\*For number previously paid, if greater. For Reissues, see above

<b>Complete if Known</b>	
Application Number	
Filing Date	
First Named Inventor	Samuel Pedro Goldman
Examiner Name	
Art Unit	
Attorney Docket No.	9611-35

## FEE CALCULATION (continued)

## 3. ADDITIONAL FEES

Large Entity Small Entity

Fee Code (\$)	Fee Code (\$)	Fee Description	Fee Paid
1051 130	2051 65	Surcharge - late filing fee or oath	
1052 50	2052 25	Surcharge - late provisional filing fee or cover sheet	
1053 130	1053 130	Non-English specification	
1812 2,520	1812 2,520	For filing a request for ex parte reexamination	
1804 920*	1804 920*	Requesting publication of SIR prior to Examiner action	
1805 1,840*	1805 1,840*	Requesting publication of SIR after Examiner action	
1251 110	2251 55	Extension for reply within first month	
1252 420	2252 210	Extension for reply within second month	
1253 950	2253 475	Extension for reply within third month	
1254 1,480	2254 740	Extension for reply within fourth month	
1255 2,010	2255 1,005	Extension for reply within fifth month	
1401 330	2401 165	Notice of Appeal	
1402 330	2402 165	Filing a brief in support of an appeal	
1403 290	2403 145	Request for oral hearing	
1451 1,510	1451 1,510	Petition to institute a public use proceeding	
1452 110	2452 55	Petition to revive - unavoidable	
1453 1,330	2453 665	Petition to revive - unintentional	
1501 1,330	2501 665	Utility issue fee (or reissue)	
1502 480	2502 240	Design issue fee	
1503 840	2503 320	Plant issue fee	
1460 130	1460 130	Petitions to the Commissioner	
1807 50	1807 50	Processing fee under 37 CFR 1.17(q)	
1808 180	1808 180	Submission of Information Disclosure Stmt	
8021 40	8021 40	Recording each patent assignment per property (times number of properties)	
1809 770	2808 385	Filing a submission after final rejection (37 CFR 1.129(a))	
1810 770	2810 385	For each additional invention to be examined (37 CFR 1.129(b))	
1801 770	2801 385	Request for Continued Examination (RCE)	
1802 600	1802 600	Request for expedited examination of a design application	
Other fee (specify)			
*Reduced by Basic Filing Fee Paid			
<b>SUBTOTAL (3)</b>		<b>(\$ 0.00)</b>	

(Complete if applicable)	
Name (Print/Type)	Timothy J. Shinnott
Signature	
Registration No. /Attorney/Agent	31,083
Telephone	(416) 364-7311
Date	December 12, 2003

WARNING: Information on this form may become public. Credit card information should not be included on this form. Provide credit card information and authorization on PTO-2038.

This collection of information is required by 37 CFR 1.17 and 1.27. The information is required to obtain or retain a benefit by the public which is to file (and by the USPTO to process) an application. Confidentiality is governed by 35 U.S.C. 122 and 37 CFR 1.14. This collection is estimated to take 12 minutes to complete, including gathering, preparing, and submitting the completed application form to the USPTO. Time will vary depending upon the individual case. Any comments on the amount of time you require to complete this form and/or suggestions for reducing this burden, should be sent to the Chief Information Officer, U.S. Patent and Trademark Office, U.S. Department of Commerce, P.O. Box 1450, Alexandria, VA 22313-1450. DO NOT SEND FEES OR COMPLETED FORMS TO THIS ADDRESS.

**Patent Application Data Sheet****Application Information**

**Application Type::** Provisional  
**Subject Matter::** Utility  
**Suggested Classification::**  
**Suggested Group Art**  
**Unit::**  
**Title::** FAST INVERSE DOSE OPTIMIZATION  
**Attorney Docket Number::** 9611-35  
**Request for Early Publication?::** No  
**Request for Non-Publication?::** No  
**Suggested Drawing Figure::**  
**Total Drawing Sheets::**  
**Small Entity?::** Yes

**Applicant Information**

**Inventor Authority Type::** Inventor

**Primary Citizenship**  
**Country::** Canadian  
**Status::** Full Capacity

**Given Name::** Samuel  
**Middle Name::** Pedro

Family Name:: Goldman  
Name Suffix::  
City of Residence:: London  
State or Prov. Of Residence:: Ontario  
Country of Residence:: Canada  
Street of mailing address:: 1144 Quinton Road  
City of mailing address:: London  
State or Province of mailing address:: Ontario  
Country of mailing address:: Canada  
Postal or Zip Code of mailing address:: N6H 4R1

Inventor Authority Type:: Inventor

Primary Citizenship  
Country:: Canadian  
Status:: Full Capacity

Given Name:: Jerry  
Middle Name:: J.  
Family Name:: Battista  
Name Suffix::  
City of Residence:: London  
State or Prov. Of Residence:: Ontario  
Country of Residence:: Canada  
Street of mailing address:: 87 Orkney Crescent  
City of mailing address:: London

**State or Province of**  
**mailing address::** Ontario  
**Country of mailing address::** Canada  
**Postal or Zip Code of**  
**mailing address::** N5X 3R8

**Inventor Authority Type::** Inventor

**Primary Citizenship**

**Country::** Canadian  
**Status::** Full Capacity

**Given Name::** Jeff  
**Middle Name::** Z.  
**Family Name::** Chen  
**Name Suffix::**  
**City of Residence::** London  
**State or Prov. Of**  
**Residence::** Ontario  
**Country of Residence::** Canada  
**Street of mailing address::** 134 Laurel Street  
**City of mailing address::** London  
**State or Province of**  
**mailing address::** Ontario  
**Country of mailing address::** Canada  
**Postal or Zip Code of**  
**mailing address::** N6H 4X1

**Correspondence Information****Correspondence Customer**

Number:: 001059  
Phone Number:: (416) 364-7311

Fax Number:: (416) 381-1398

E-Mail Address:: tsinnot@bereskinparr.com

**Representative Information**

Representative	
Customer Number::	001059

**THIS PAGE IS INSERTED BY OIPE SCANNING  
AND IS NOT PART OF THE OFFICIAL RECORD**

**Best Available Images**

Defective images within this document are accurate representations of the original documents submitted by the applicant.

Defects in the images may include (but are not limited to):

**BLACK BORDERS**

**TEXT CUT OFF AT TOP, BOTTOM OR SIDES**

**FADED TEXT**

**BLURRY OR ILLEGIBLE TEXT**

**SKEWED/SLANTED IMAGES**

**COLORED PHOTOS HAVE BEEN RENDERED INTO BLACK AND WHITE**

**VERY DARK BLACK AND WHITE PHOTOS**

**UNDECIPHERABLE GRAY SCALE DOCUMENTS**

**IMAGES ARE THE BEST AVAILABLE  
COPY. AS RESCANNING *WILL NOT*  
CORRECT IMAGES, PLEASE DO NOT  
REPORT THE IMAGES TO THE  
PROBLEM IMAGE BOX.**

PATENT APPLICATION SERIAL NO. \_\_\_\_\_

U.S. DEPARTMENT OF COMMERCE  
PATENT AND TRADEMARK OFFICE  
FEE RECORD SHEET

12/16/2003 FMETEKI1 0000006 022095 60528775

01 FC:2005 80.00 DA

PTO-1556  
(5/87)

\*U.S. Government Printing Office: 2002 — 489-267/69033

B&P File No. 9611-35

**BERESKIN & PARR**

**UNITED STATES**  
**PROVISIONAL APPLICATION**

**Title: Fast Inverse Dose Optimization**

**Inventors: Samuel Pedro Goldman, Jerry J. Battista and Jeff Z. Chen**

**FIDO - Fast Inverse Dose Optimization**  
***Detailed Description of Invention***

The most fundamental requirements of a radiation treatment optimization are: (i) dose is homogeneously deposited in the Planning Target Volume (PTV); (ii) the dose deposited in any Organ At Risk (OAR) does not exceed a threshold value and ideally should be zero; (iii) the dose deposited in All The Rest (ATR), i.e. organs and tissue not included in the PTV and OARs, should be as small as possible and ideally zero to minimize the risk of secondary carcinogenesis; (iv) the dose gradient crossing the PTV boundaries should be as high as possible. Optimizations are pursued by the minimization of a positive-definite objective function. A successful optimization will yield a global minimum to this objective function in a short computation time with physically achievable beamlet intensities.

This work presents a new approach to radiation treatment optimization that is very fast and yields a global minimum of the objective function without the use of a search routine but rather solves a linear system of equations. The possibility of such a direct optimization scheme has been known for decades but it has been impossible to implement rigorously using conventional quadratic objective functions because optimized results are only achievable with unphysical negative beamlet intensities [3]. Once an ad-hoc condition requiring the beamlet intensities to be positive is introduced (i.e. force negative values to be zero), the linear method yields a dose distribution with artifacts. Alternatively, one may pursue a minimum of the objective function by a direct search over all possible positive beam intensities, but this is a very time-consuming approach. In our work the negative-intensities problem is dealt with *within the objective function* and not as an externally imposed ad-hoc requirement.

We summarize now our approach. In the following we call "organ" any organ, target volume, region of tissue, identifiable anatomical entity or any defined volume within the volume exposed to radiation. For simplicity we will divide the set of organs into organs that must receive a certain dose and organs that should receive no dose or a dose as small as possible. A typical objective function  $O$  satisfying the optimization conditions stated above is of the form:

$$O = \sum_i p_i^{d_{req}} O_i^{d_{req}} + \sum_m p_m^{no-dose} O_m^{no-dose}$$

where the  $p_i$  are importance coefficients and the objectivity terms are:

$$O_i^{d_{req}} = \sum_{x \in \text{organ}_i} \left( \sum_j w_j d_j(x) - d^{req} \right)^2$$

$$O_m^{no-dose} = \sum_{x \in \text{organ}_m} \left( \sum_j w_j d_j(x) \right)^2$$

where  $w_i$  is the weight of beamlet  $i$ ,  $d_i$  is the dose deposited at destination point  $x$  by beamlet  $i$  and  $d^{req}$  is the dose required in organ  $i$ .

The main reason for the traditional appearance of negative weights upon optimization of the objective function  $O$  is the fact that we require satisfying two conflicting demands: on one hand we require  $O_{ATR} = 0$  and on the other we require radiation to pass through the ATR (and possibly OARs) to reach the PTV. A correct requirement on  $O_{ATR}$  (and OARs) is that  $O^{no-dose}$  should be minimized and  $O^{d_{req}}$  should be zero only if the weights of all the beamlets passing through the "no-dose" organs are zero. This requirement is satisfied if instead of that standard  $O^{no-dose}$  above, we use new terms of the form

## Detailed Description of Invention

$$\tilde{O}_n^{co-dec} = \sum_{\text{organs}} \sum_{i}^{\text{all beamlets}} w_i^2 d_i^2(x)$$

\*\*\*\*\*novel idea\*\*\*\*\*

We have as well added another term to the objective function that replaces the unrealistic zero-limit for the beamlet weights with an equal-weight limit (cylindrical symmetry) which is usually the initial set of weights before optimization. This term is of the form

$$O^{eq} = \sum_i^{\text{all beamlets}} (w_i^2 - w_i).$$

\*\*\*\*\*novel idea\*\*\*\*\*

With the weights normalized to

$$\sum_i^{\text{all beamlets}} w_i = \text{total number of beamlets},$$

$O^{eq}$  is positive and its minimum is zero when  $w_i = 1$  for all  $i$ .  $O^{eq}$  provides the most powerful constraint to avoid negative weights.

With the new terms introduced above, the new objective function to be used is of the form:

$$O = \sum_{\text{organs with required dose}} p_{\text{A}}^{dec} O_{\text{A}}^{dec} + \sum_{\text{organs without required dose}} \tilde{p}_{\text{A}}^{co-dec} \tilde{O}_{\text{A}}^{co-dec} + p_{eq} O^{eq}$$

\*\*\*\*\*novel idea\*\*\*\*\*

Although not necessary (and in general counterproductive) the terms  $O_{\text{A}}^{no-dec}$  can also be added to the objective function. In our calculations, the terms  $O_{\text{A}}^{no-dec}$  were given non-zero importance coefficients when we wanted to demonstrate the appearance of negative weights upon optimization. With this consideration a more general objective function is:

$$O = \sum_{\text{A}} p_{\text{A}}^{dec} O_{\text{A}}^{dec} + \sum_{\text{A}} \tilde{p}_{\text{A}}^{co-dec} \tilde{O}_{\text{A}}^{co-dec} + p_{eq} O^{eq} + \sum_{\text{A}} p_{\text{A}}^{no-dec} O_{\text{A}}^{no-dec}.$$

\*\*\*\*\*novel idea\*\*\*\*\*

Where the coefficients  $p_{\text{A}}$  are the importance parameters for organ  $\text{A}$  within an objectivity component and  $p_{eq}$  is the importance parameter of the asymptotic symmetry condition. The optimization problem for all the beam intensities is reduced to the solution of a linear system of equations as is shown in the following paragraphs.

The optimum of the objective function is obtained by minimizing the objective function from the system of equations:

The optimum of the positive-definite objective function  $O$  is obtained by minimizing  $O$  with respect to all the weights  $w_i$ . We perform this minimization by requiring the set of first derivatives of  $O$  to satisfy:

$$0 = \frac{\partial O}{\partial w_j} \quad \text{for all } w_j.$$

Consider the term  $O_{\text{A}}^{dec}$ :

$$\frac{\partial O_{\text{A}}^{dec}}{\partial w_j} = 2 \sum_{\text{organs}} d_i(x) \left( \sum_i^{\text{all beamlets}} w_i d_i(x) - d^{req, \text{A}} \right)$$

## Detailed Description of Invention

In our novel approach, we exchange the order of the summations to obtain:

$$\frac{\delta O_k^{dec}}{\delta w_j} = 2 \sum_i^{\text{all beamlets}} w_i \left( \sum_{x \in \text{beamlet}_i} d_i(x) d_j(x) \right) - 2 d_i^{org, k} \sum_{x \in \text{beamlet}_i} d_j(x) \quad \text{oooo\_novel idea\_oooo}$$

This simple exchange in the summation order simplifies enormously the problem! We are now able to formulate the problem only in terms of the beamlet weights. The  $x$ -dependence (destination point dependence) has been eliminated by summing over all destination points in advance. We can define now the  $x$ -independent arrays:

$$\alpha_{ij}^{org, k} = \sum_{x \in \text{beamlet}_i} d_i(x) d_j(x) \quad \text{oooo\_novel idea\_oooo}$$

and

$$\beta_j^{org, k} = d_i^{org, k} \sum_{x \in \text{beamlet}_i} d_j(x) \quad \text{oooo\_novel idea\_oooo}$$

The optimization problem for the optimal weights  $w_i$  is given by the solution to the system of linear algebraic equations:

$$\sum_j^{\text{all beamlets}} \alpha_{ij} w_j = \beta_i \quad \text{oooo\_novel idea\_oooo}$$

where

$$\alpha_{ij} = \sum_b^{\text{all organs with required data}} p_b^{dec} \alpha_{ij}^{org, k} + \sum_m^{\text{all organs without required data}} p_m^{no-dec} \alpha_{ij}^{org, k} + \sum_n^{\text{all organs without required data}} \bar{p}_n^{no-dec} \alpha_{ij}^{org, k} \delta_{ij} + p_{org} \delta_{ij} \quad \text{oooo\_novel idea\_oooo}$$

and

$$\beta_i = \sum_b^{\text{all organs with required data}} p_b^{dec} \beta_i^{org, k} + \frac{1}{2} p_{org} \quad \text{oooo\_novel idea\_oooo}$$

The solution to the optimization problem is obtained by the numerical inversion of the matrix  $\alpha_{ij}$ :

$$w_i = \sum_j^{\text{all beamlets}} \alpha_{ij}^{-1} \beta_j \quad \text{oooo\_novel idea\_oooo}$$

# Fast Inverse Dose Optimization (FIDO) for IMRT via Matrix Inversion with no Negative Intensities

S. P. Goldman<sup>1</sup>, J. Z. Chen<sup>1</sup> and J. J. Battista<sup>2</sup>

<sup>1</sup>Dept. of Physics & Astronomy, University of Western Ontario, London, Ontario, Canada

<sup>2</sup>Dept. of Oncology, University of Western Ontario and London Regional Cancer Centre, London, Ontario Canada

## Abstract

A fast optimization algorithm is very important for inverse planning of Intensity Modulated Radiation Therapy (IMRT), and for adaptive radiotherapy of the future. Conventional numerical search algorithms such as the conjugate gradient search, conducted with positive beam weight constraints, generally require many iterations and may produce suboptimal results due to trapping in local minima. A direct solution of the inverse problem using conventional quadratic objective functions without positive beam constraints is more efficient but will result in unrealistic negative beam weights. We present here a direct solution of the inverse problem which does not result in unacceptable negative beam weights. The objective function for the optimization of beam intensities for large number of beamlets is reformulated such that the optimization problem is reduced to a linear set of equations. The optimal set of intensities is found through a matrix inversion, and negative beamlet intensities are avoided without the need for externally imposed constraints. The method has been applied to a test phantom and to a few clinical cases. We were able to achieve highly conformal dose distributions with very short optimization times. Typical optimization times for a single anatomical slice using a single processor desktop computer are: 0.2 sec. for 400 beamlets; 8 sec. for 1,000 beamlets; 40 sec. for 2,000 beamlets and 2.5 min for 3,000 beamlets. These times can be substantially further improved using a better optimization routine for matrix inversion. In conclusion, the new method provides a fast and robust technique to find a global minimum that yields excellent results for the inverse planning of IMRT.

## Keywords

Inverse planning, optimization, objective function.

## Introduction

Intensity Modulated Radiation Therapy (IMRT) is becoming a new standard for radiotherapy. Given the better conformal dose distributions obtained through IMRT and its dynamic delivery features, adaptive radiotherapy becomes an important factor to be considered. A fast optimization algorithm is crucial not only for designing good radiation treatment plans but also for the successful implementation of future interactive adaptive treatment techniques. Conventional optimization algorithms using numerical searches such as the conjugate gradient search [1-2] with positive beam weight constraints usually require many iterations (i.e. long computation times) and may result in suboptimal plans due to trapping in local minima of the objective function. A direct solution of the inverse problem using conventional quadratic objective functions without imposing positive beam constraints will be computationally faster but will result in unrealistic negative beam weights. We present here a very fast method for the direct solution of the inverse problem (FIDO) that avoids the difficulty of negative beam weights and preserves efficiency.

## Method

The most fundamental requirements of a radiation treatment optimization are: (i) dose is homogeneously deposited in the Planning Target Volume (PTV); (ii) the dose deposited in any Organ At Risk (OAR) does not exceed a threshold value and

ideally should be zero; (iii) the dose deposited in All The Rest (ATR), i.e. organs and tissue not included in the PTV and OARs, should be as small as possible and ideally zero to minimize the risk of secondary carcinogenesis; (iv) the dose gradient crossing the PTV boundaries should be as high as possible. Optimizations are pursued by the minimization of a positive-definite objective function. A successful optimization will yield a global minimum to this objective function in a short computation time with physically achievable beamlet intensities.

This work presents a new approach to radiation treatment optimization that is very fast and yields a global minimum of the objective function without the use of a search routine but rather solves a linear system of equations. The possibility of such a direct optimization scheme has been known for decades but it has been impossible to implement rigorously using conventional quadratic objective functions because optimized results are only achievable with unphysical negative beamlet intensities [3]. Once an ad-hoc condition requiring the beamlet intensities to be positive is introduced (i.e. force negative values to be zero), the linear method yields a dose distribution with artefacts. Alternatively, one may pursue a minimum of the objective function by a direct search over all possible positive beam intensities, but this is a very time-consuming approach. In our work the negative-intensities problem is dealt with *within the objective function* and not as an externally imposed ad-hoc requirement.

We summarize now our approach. For simplicity we will consider a single PTV, a single OAR and a single ATR. A typical objective function  $O$  satisfying the optimization conditions stated above is of the form:

$$O = p_{PTV}O_{PTV} + p_{OAR}O_{OAR} + p_{ATR}O_{ATR}$$

where the  $p_i$  are importance coefficients and the objective terms are:

$$O_{PTV} = \sum_{x \in PTV} \left( \sum_i^{\text{all beamlets}} w_i d_i(x) - d^{PTV} \right)^2,$$

$$O_{OAR} = \sum_{x \in OAR} \left( \sum_i^{\text{all beamlets}} w_i d_i(x) \right)^2,$$

and  $O_{ATR} = \sum_{x \in ATR} \left( \sum_i^{\text{all beamlets}} w_i d_i(x) \right)^2$ .

where  $w_i$  is the weight of beamlet  $i$ ,  $d_i$  is the dose deposited at destination point  $x$  by beamlet  $i$  and  $d^{PTV}$  is the dose prescribed to the PTV. The main reason for the traditional appearance of negative weights upon optimization of the objective function  $O$  is the fact that we require satisfying two conflicting demands: on one hand we require  $O_{ATR} = 0$  and on the other we require radiation to pass through the ATR (and possibly OARs) to reach the PTV. A correct requirement on  $O_{ATR}$  is that  $O_{ATR}$  should be minimized and  $O_{ATR}$  should be zero only if the weights of all the beamlets passing through the ATR are zero. This requirement is satisfied if instead of  $O_{ATR}$  we use a new ATR term of the form

$$\tilde{O}_{ATR} = \sum_{x \in ATR} \sum_i^{\text{all beamlets}} w_i^2 d_i^2(x).$$

Similarly for the OAR we use:

$$\tilde{O}_{OAR} = \sum_{x \in OAR} \sum_i^{\text{all beamlets}} w_i^2 d_i^2(x).$$

We have as well added another term to the objective function that replaces the unrealistic zero-limit for the beamlet weights with an equal-weight limit (cylindrical symmetry) which is usually the initial set of weights before optimization. This term is of the form

$$O_{sym} = \sum_i^{\text{all beamlets}} (w_i^2 - w_i).$$

With the weights normalized to

$$\sum_i^{\text{all beamlets}} w_i = \text{total number of beamlets},$$

$O_{sym}$  is positive and its minimum is zero when  $w_i = 1$  for all  $i$ . With these modifications, the optimization problem for all the beam intensities is reduced again to the solution of a linear system of equations of the form:

$$\sum_j \alpha_{ij} w_j = \beta_i \quad (1)$$

where  $w_j$  is the (unknown) weight or intensity of beamlet  $j$ ,  $\beta_i$  is a vector of coefficients that depends on the dose deposited by beam  $i$  within the PTV, and  $\alpha_{ij}$  is a matrix that describes the product of the doses deposited by the intersecting pairs of beamlets  $i$  and  $j$  on different organs (each organ with its importance coefficient). The set of optimal beam weights is obtained from (1) by inversion:

$$w_i = \sum_j \alpha_{ij}^{-1} \beta_i$$

In other words, the solution to the (large) system of linear equations (1) is obtained quickly and accurately by inverting the array  $\alpha_{ij}$  using standard matrix inversion routines.

### Results

Below we present several sets of preliminary results obtained with this technique for a prostate case, a head and neck case, and an "interlocked rectangles" phantom on a 2D slice. Only primary KERMA has been included in the calculations reported here, but very similar results are obtained in dose distributions, when the calculated beam intensities are imported to a commercial treatment planning system (Theraplan Plus V3.8, Nucletron). The only difference is a slightly diffused dose to the OARs due to scatter spreading effects. In each case, we include calculation and optimization times for KERMA calculations as they were obtained on a single-processor desktop PC. The program was written in C# using the Microsoft .NET environment. The matrix inversion routine was obtained from *Numerical Recipes* [4] and translated from FORTRAN into C#. No effort has been devoted to maximize the speed of the matrix inversion procedure.

In all cases the number of gantry angles used is evenly distributed over a full 360 degree circle around the isocentre. Each beam is evenly divided into beamlets of the specified width resulting in the total number of beamlets quoted. The source to axis distance (SAD) is 100 cm. In each case we also present the DVH, scaled to 100% volume on the vertical axis and 100% dose on the horizontal axis, and a colour-coded dose deposition map with blue showing no dose deposition (primary KERMA only) and red the largest dose deposition.

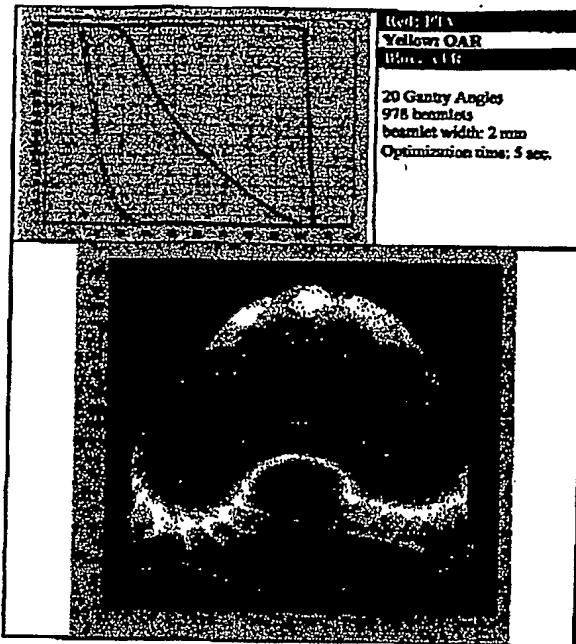
### Conclusions and future work

We have developed a fast and robust technique to find a global minimum that yields excellent results for the inverse optimization problem for the radiation treatment of tumours, using large sets of non-negative intensity-modulated beamlets.

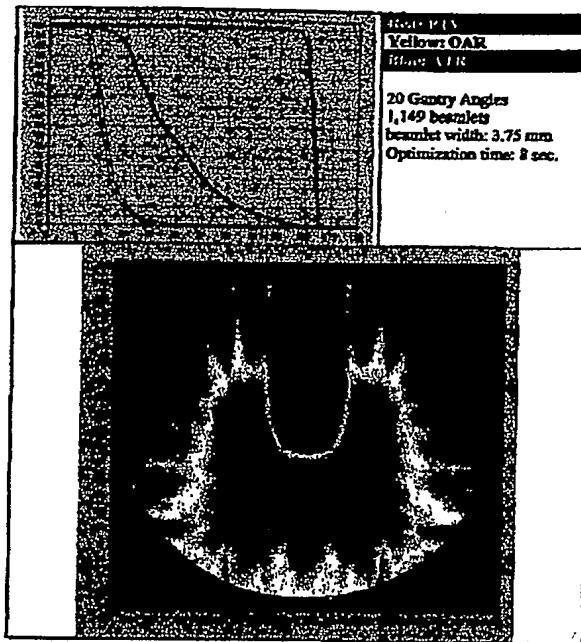
Work is currently in progress on a full implementation FIDO in our treatment planning system that uses collapsed cone convolution method for dose calculation [5]. Work is proceeding as well on an efficient 3D implementation for on-line adaptive radiotherapy as might be possible with helical tomotherapy [6].

The authors would like to thank the following agencies for their financial support during this work: The National Sciences and Engineering Research Council of Canada and the Ontario Research and Development Challenge Fund (OCITS project). We also would like to thank Dr. E. Wong for useful discussions and for suggesting the challenging geometry of the interlocked rectangle phantom.

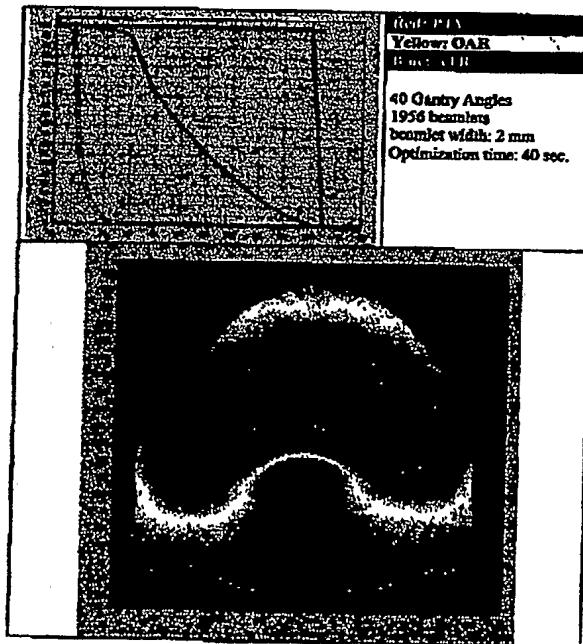
**Figure 1: Head and Neck Case. - 20 gantry angles**



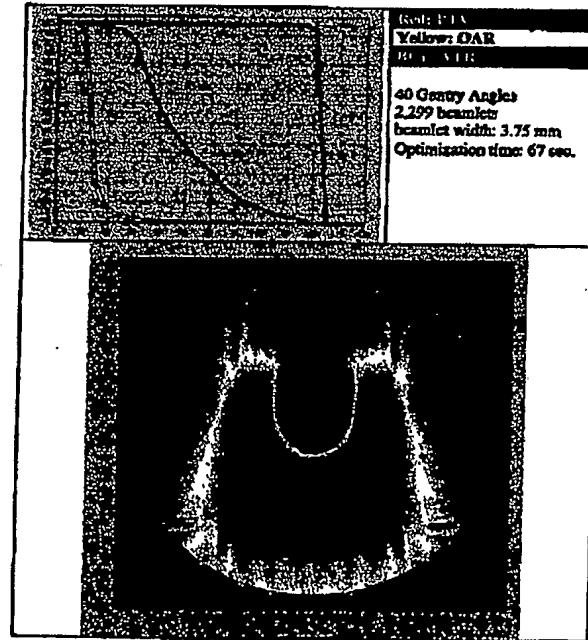
**Figure 3: Interlocked Rectangles Phantom. - 20 gantry angles**

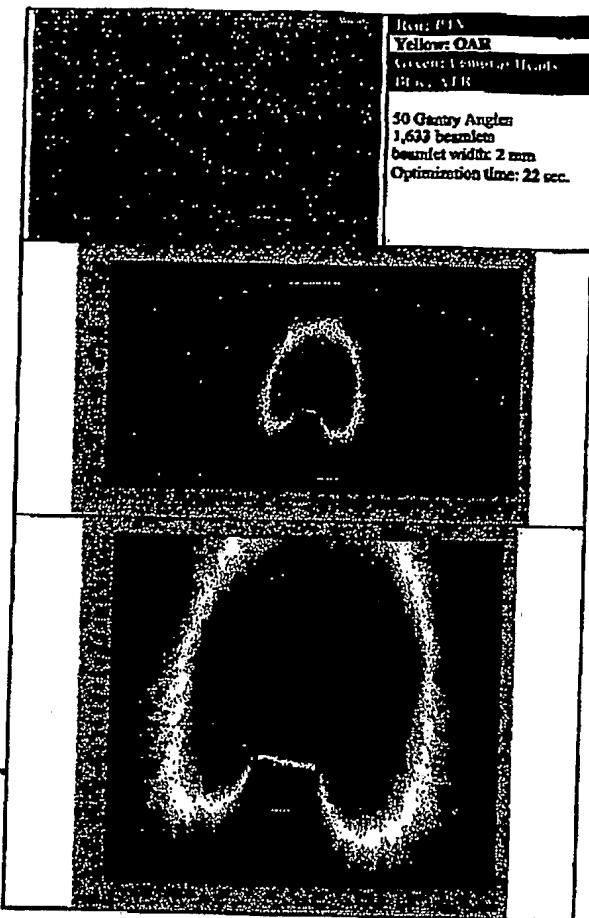


**Figure 2: Head and Neck Case. - 40 gantry angles**



**Set No. 4: Interlocked Rectangles. - 40 gantry angles**



**Set No. 5: Prostate Case (Panoramic and close-up views).****References**

- [1] S. Smith and L. S. Lasdon, "Solving large sparse nonlinear programs using GRG ORSA", *Journal on Computing*, 4, 1-15 (1992).
- [2] S. V. Spirou and C. S. Chui, "A gradient inverse planning algorithm with dose-volume constraints", *Med Phys.* 25(3), 321-33 (1998).
- [3] S. Webb, "The physical basis of IMRT and inverse planning", *Br J Radiol.* 76(910), 678-89, Review (2003).
- [4] Press W H, Flannery B P, Vetterling W T and Teukolsky S A, "Numerical Recipes" (Cambridge University Press).
- [5] A. Ahnesjo, "Collapsed cone convolution of radiant energy for photon dose calculation in heterogeneous media", *Med. Phys.* 16, 577-592 (1989).
- [6] T. R. Mackie, J. Balog, K. Ruchala, D. Shepard, S. Aldridge, E. Fichard, P. Reckwerdt, G. Olivera, T. McNutt, M. Mehta, "Tomotherapy", *Semin Radiat Oncol.* 9(1), 108-117 (1999).

**We claim:**

1. A method for optimizing radiation treatment, said method comprising the step of resolving an objective function, said objective function comprising importance coefficients and objectivity terms.
2. A system for optimizing radiation treatment, said system comprising means for resolving an objective function.
3. A method of planning delivery of radiation therapy to maximize radiation to a planned target volume and minimize radiation to surrounding tissues outside the planned target volume, said method comprising the step of resolving an objective function.
4. The invention substantially as described and illustrated herein.